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WHAT IS CLAIMED IS:

- 1. A method for determining the square root of a long-bit number using a short-bit processor, comprising the steps of:
- (A) assuming the long-bit number to be $c \times 2^{2K} + d$, where c, $d < 2^{2k}$, and its solution to be $(a \times 2^K + b)^2$;
 - (B) finding 'a' by using a bisection method to obtain the floor value of the square root of 'c';
 - (C) rearranging and transforming the equations in step (A) to obtain a successive substitution equation: $b_{[n]} = (c-a^2) \times 2^{2k} + (d-b_{[n-1]}^2) / 2^{2(k+1)}$; and
 - (D) giving an initial value to 'b' to execute the successive substitution equation recursively several times until the equation is convergent, thereby finding 'b'.
 - 2. The method as claimed in claim 1, wherein, in step (B), the bisection method is used to find a maximum value of 'a' that satisfies the condition of $a^2 < c$.
 - 3. The method as claimed in claim 1, wherein, in step (D), the initial value of 'b' is 0.
- 4. The method as claimed in claim 1, wherein, in step (D), the successive substitution equation is executed recursively for three times.
 - 5. A method for determining the square root of a long-bit number using a short-bit processor, comprising the steps of:
- (A) assuming the long-bit number to be $c \times 2^{2K} + d$, where c, $d < 2^{2k}$, and its solution to be $(a \times 2^K + b)^2$;
 - (B) determining the solution by respectively finding the value of

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'a' and 'b';

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- (C) finding 'a' by taking the floor value of the square root of 'c';
- (D) rearranging and transforming the equations in step (A) to obtain a successive substitution equation: $b_{[n]} = (c-a^2) \times 2^{2k} + (d-b_{[n-1]}^2) / 2^{2(k+1)}$; and
- (E) giving an initial value to 'b' to execute the successive substitution equation recursively for several times until the equation is convergent, thereby finding 'b'.
- 6. The method as claimed in claim 5, wherein, in step (C), a

 bisection method is used to find a maximum value of 'a' that satisfies the condition of a² <c.
 - 7. The method as claimed in claim 5, wherein, in step (E), the initial value of 'b' is 0.
 - 8. The method as claimed in claim 5, wherein, in step (E), the successive substitution equation is executed recursively for three times.